## **Trigonometry**

1

Fig. 10.1 shows Jean's back garden. This is a quadrilateral ABCD with dimensions as shown.

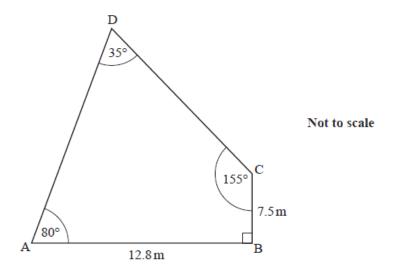


Fig. 10.1

(i) (A) Calculate AC and angle ACB. Hence calculate AD.

[6]

(B) Calculate the area of the garden.

[3]

2

Fig. 7 shows a sketch of a village green ABC which is bounded by three straight roads.  $AB = 92 \, \text{m}$ ,  $BC = 75 \, \text{m}$  and  $AC = 105 \, \text{m}$ .

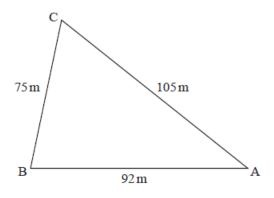


Fig. 7

Calculate the area of the village green.

## Algebra and graphs

3

Make r the subject of the formula  $A = \pi r^2(x+y)$ , where r > 0. [2]

4

Make x the subject of the equation 
$$y = \frac{x+3}{x-2}$$
. [4]

5

A line L is parallel to y = 4x + 5 and passes through the point (-1,6). Find the equation of the line L in the form y = ax + b. Find also the coordinates of its intersections with the axes. [5]

6

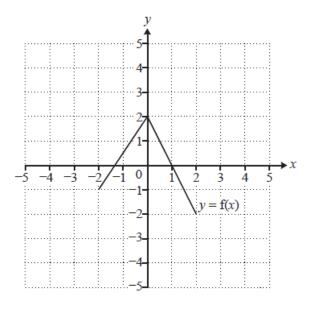


Fig. 3

Fig. 3 shows the graph of y = f(x). Draw the graphs of the following.

(i) 
$$y = f(x) - 2$$

(ii) 
$$y = f(x-3)$$

7

The point R(6, -3) is on the curve y = f(x).

- (i) Find the coordinates of the image of R when the curve is transformed to  $y = \frac{1}{2}f(x)$ . [2]
- (ii) Find the coordinates of the image of R when the curve is transformed to y = f(3x). [2]

8

Find the coordinates of the point of intersection of the lines y = 5x - 2 and x + 3y = 8. [4]

## **Indices and surds**

9

Evaluate the following.

(ii) 
$$\left(\frac{25}{9}\right)^{-\frac{1}{2}}$$

10

(i) Evaluate 
$$\left(\frac{1}{27}\right)^{\frac{2}{3}}$$
. [2]

(ii) Simplify 
$$\frac{(4a^2c)^3}{32a^4c^7}$$
. [3]

11

(i) Expand and simplify 
$$(3+4\sqrt{5})(3-2\sqrt{5})$$
. [3]

(ii) Express 
$$\sqrt{72} + \frac{32}{\sqrt{2}}$$
 in the form  $a\sqrt{b}$ , where  $a$  and  $b$  are integers and  $b$  is as small as possible. [2]

## **Inequalities**

12

Solve the inequality 
$$\frac{4x-5}{7} > 2x+1$$
. [3]

Solve the inequality 
$$3x^2 + 10x + 3 > 0$$
. [3]

## Quadratics and their graphs

#### 14

Fig. 8 shows a right-angled triangle with base 2x + 1, height h and hypotenuse 3x.

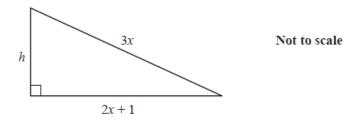


Fig. 8

- (i) Show that  $h^2 = 5x^2 4x 1$ . [2]
- (ii) Given that  $h = \sqrt{7}$ , find the value of x, giving your answer in surd form. [3]

15

- (i) Express  $x^2 5x + 6$  in the form  $(x a)^2 b$ . Hence state the coordinates of the turning point of the curve  $y = x^2 5x + 6$ .
- (ii) Find the coordinates of the intersections of the curve  $y = x^2 5x + 6$  with the axes and sketch this curve. [4]

16

Express 
$$3x^2 - 12x + 5$$
 in the form  $a(x - b)^2 - c$ . Hence state the minimum value of  $y$  on the curve  $y = 3x^2 - 12x + 5$ .

#### **Proof**

#### **17**

Factorise  $n^3 + 3n^2 + 2n$ . Hence prove that, when n is a positive integer,  $n^3 + 3n^2 + 2n$  is always divisible by 6.

18

n-1, n and n+1 are any three consecutive integers.

- (i) Show that the sum of these integers is always divisible by 3. [1]
- (ii) Find the sum of the squares of these three consecutive integers and explain how this shows that the sum of the squares of any three consecutive integers is never divisible by 3.[3]

#### Longer questions on graphs

19

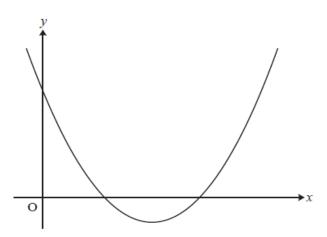


Fig. 11

Fig. 11 shows a sketch of the curve with equation  $y = (x-4)^2 - 3$ .

- (i) Write down the equation of the line of symmetry of the curve and the coordinates of the minimum point.
- (ii) Find the coordinates of the points of intersection of the curve with the x-axis and the y-axis, using surds where necessary.
- (iii) The curve is translated by  $\binom{2}{0}$ . Show that the equation of the translated curve may be written as  $y = x^2 12x + 33$ .

20

You are given that f(x) = (x+3)(x-2)(x-5).

(i) Sketch the curve 
$$y = f(x)$$
. [3]

- (ii) Show that f(x) may be written as  $x^3 4x^2 11x + 30$ . [2]
- (iii) Describe fully the transformation that maps the graph of y = f(x) onto the graph of y = g(x), where  $g(x) = x^3 4x^2 11x 6$ . [2]

## Statistics and probability

1 The ages, x years, of the senior members of a running club are summarised in the table below.

Age (x)	20 ≤ <i>x</i> < 30	30 ≤ <i>x</i> < 40	40 ≤ <i>x</i> < 50	50 ≤ <i>x</i> < 60	$60 \leqslant x < 70$	$70 \leqslant x < 80$	80 ≤ <i>x</i> < 90
Frequency	10	30	42	23	9	5	1

Draw a cumulative frequency diagram to illustrate the data.

[5]

(ii) Use your diagram to estimate the median and interquartile range of the data.

[3]

2

Candidates applying for jobs in a large company take an aptitude test, as a result of which they are either accepted, rejected or retested, with probabilities 0.2, 0.5 and 0.3 respectively. When a candidate is retested for the first time, the three possible outcomes and their probabilities remain the same as for the original test. When a candidate is retested for the second time there are just two possible outcomes, accepted or rejected, with probabilities 0.4 and 0.6 respectively.

(i) Draw a probability tree diagram to illustrate the outcomes.

[3]

(ii) Find the probability that a randomly selected candidate is accepted.

[2]

(iii) Find the probability that a randomly selected candidate is retested at least once, given that this candidate is accepted.

3

Each weekday, Marta travels to school by bus. Sometimes she arrives late.

- L is the event that Marta arrives late.
- R is the event that it is raining.

You are given that P(L) = 0.15, P(R) = 0.22 and P(L | R) = 0.45.

(i) Use this information to show that the events L and R are not independent.

[1]

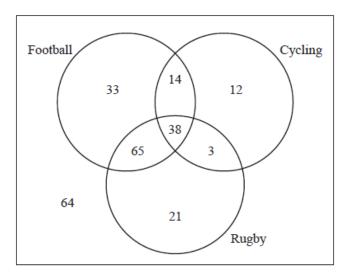
(ii) Find 
$$P(L \cap R)$$
. [2]

(iii) Draw a Venn diagram showing the events L and R, and fill in the probability corresponding to each of the four regions of your diagram.[3]

A survey is being carried out into the sports viewing habits of people in a particular area. As part of the survey, 250 people are asked which of the following sports they have watched on television in the past month.

- Football
- Cycling
- Rugby

The numbers of people who have watched these sports are shown in the Venn diagram.



One of the people is selected at random.

(i) Find the probability that this person has in the past month

(B) watched either one or two of the three sports. [2]

(ii) Given that this person has watched cycling, find the probability that this person has not watched football.
[2]

## **Kinematic graphs**

5

Fig. 1 shows the velocity-time graph of a cyclist travelling along a straight horizontal road between two sets of traffic lights. The velocity, v, is measured in metres per second and the time, t, in seconds. The distance travelled, s metres, is measured from when t = 0.

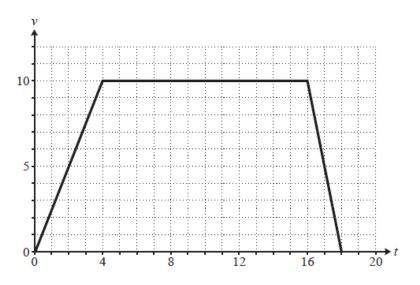


Fig. 1

(i) Find the values of s when t = 4 and when t = 18.

[3]

(ii) Sketch the graph of s against t for  $0 \le t \le 18$ .

[3]

Questi	on	Answer	Marks	Guidan	ice
(i)	(A)	$AC^2 = 12.8^2 + 7.5^2$ oe	M1	allow correct application of cosine rule or from finding relevant angle and using trig	
		AC = 14.83543056	A1	rot to 3 or more sf, or 15	B2 for 14.8 or better unsupported
		$\tan C = {}^{12.8}/_{7.5}$	M1	or $\sin C = {}^{12.8}/_{\text{their}14.8}$	$\operatorname{or} \frac{\sin C}{12.8} = \frac{\sin 90}{their 14.8}$
		or $C = 90 - \tan^{-1} (\frac{7.5}{12.8})$ oe		or $\cos C = \frac{7.5}{\text{their}} \frac{14.8}{\text{their}}$	or $\cos C = \frac{their 14.8^2 + 7.5^2 - 12.8^2}{2 \times 7.5 \times their 14.8}$
		59.6 to 59.64	A1		
		$\frac{AD}{\sin(155 - their 59.6)} = \frac{their 14.8}{\sin 35} \text{ oe}$	M1		
		25.69 to 25.8	A1	allow B2 for $25.69 \le AD \le 25.8$ unsupportedbut B0 for $25.8$ unsupported	<b>M0A0</b> for $^{14.8}/_{\cos 55} = 25.803$
			[6]		
<u>(i)</u>	(B)	area of ABC = 48 soi	B1	may be implied by correct final answer in range or by sight of $\frac{1}{2} \times 12.8 \times 7.5$ oe	condone 48.0
		½×their 14.8×their 25.7×sin(their 59.6 − 10)	M1	may be implied by 144.8 to 146	
		192.8 to 194[m <sup>2</sup> ]	A1		B3 for correct answer in range if unsupported
			[3]		

Answer	Marks	Guidar	nce
$\cos A = \frac{105^2 + 92^2 - 75^2}{2 \times 105 \times 92} \text{ oe}$	M1	or $\cos B = \frac{75^2 + 92^2 - 105^2}{2 \times 75 \times 92}$ oe	or $\cos C = \frac{105^2 + 75^2 - 92^2}{2 \times 105 \times 75}$ oe
0.717598soi	A1	0.2220289soi	0.519746soi
A = 44.14345° soi [0.770448553]	A1	B = 77.1717719° soi [1.346901422]	C = 58.6847827° soi [1.024242678]
			ignore minor errors due to premature rounding for second A1 condone A, B or C wrongly attributed
$\frac{1}{2} \times 92 \times 105 \times \sin (their A)$	M1	or $\frac{1}{2} \times 75 \times 92 \times \sin (their B)$	or $\frac{1}{2} \times 75 \times 105 \times \sin (their C)$
3360 or 3361 to 3365	A1		or M3 for
			$\sqrt{136(136-75)(136-105)(136-92)}$ <b>A2</b> for correct answer
	[5]		3360 or 3363 - 3364
	[5]		

Answer	Marks	Guidan	ce
$[r = ]\sqrt{\frac{A}{\pi(x+y)}}$ or $[r = ]\sqrt{\frac{A}{\pi x + \pi y}}$ as final answer	2	square root symbol must extend below fraction line; accept to power ½ with appropriate brackets  M1 for a triple decker fraction or for $r^2 = \frac{A}{\pi(x+y)} \text{ or for } [r=] \pm \sqrt{\frac{A}{\pi(x+y)}}$ or for their final answer for $r$ ft their $r^2$	condone missing end bracket in denominator
	[2]		

$y\left(x-2\right)=\left(x+3\right)$	M1	for multiplying by x – 2; condone missing brackets
xy - 2y = x + 3 or ft [ft from earlier errors if of comparable difficulty – no ft if there are no $xy$ terms]	M1	for expanding bracket and being at stage ready to collect <i>x</i> terms
xy - x = 2y + 3 or ft	M1	for collecting x and 'other' terms on opposite sides of eqn
$[x=]\frac{2y+3}{y-1} \text{ o.e. or ft}$	M1	for factorising and division

y = 4x + 10	B3	$\mathbf{M1} \text{ for } y = 4x + b \text{ oe}$
		and M1 for $y - 6 =$ their $a(x + 1)$ oe or for $(-1, 6)$ subst in $y =$ (their $a(x + 1)$ oe
		or M1 for $y = ax + 10$
(0, 10) or ft	B1	condone $y = 10$ isw
(-10/4, 0) oe or ft	B1	condone $x = -10/4$ isw
	[5]	

Question	Answer	Marks	Guida
(i)	graph of shape with vertices at $(-2, -3)$ , $(0, 0)$ and $(2, -4)$	2	M1 for 2 vertices correct
		[2]	
(ii)	graph of shape with vertices at $(1, -1)$ , $(3, 2)$ and $(5, -2)$	2	M1 for 2 vertices correct or for shape with vertices at $(-5, -1)$ , $(-3, 2)$ and $(-1, -2)$
		[2]	

(	Questio	n	Answer	Marks	Guidanc
	(i)		(6, -1.5) oe	B2	B1 for each value; allow $x = 6$ , $y = -1.5$
				[2]	
	(ii)		(2, -3)	B2	B1 for each value; allow $x = 2$ , $y = -3$
				[2]	

x + 3(5x - 2) = 8 or $y = 5(8 - 3y) - 2$	M1	for subst to eliminate one variable; condone one error;
16x = 14  or  16y = 38	M1	for collecting terms and simplifying; condoning one error ft
(7/8, 19/8) oe	<b>A</b> 2	or $x = 14/16$ , $y = 38/16$ oe isw allow <b>A1</b> for each coordinate
	[4]	

Question	n	Answer	Marks	Guidance
(i)		1	1	
			[1]	
(ii)		$\frac{3}{5}$ or 0.6	3	allow B3 for $\pm 0.6$ oe;
				M1 for $\left(\frac{25}{9}\right)^{-\frac{1}{2}} = \left(\frac{9}{25}\right)^{\frac{1}{2}}$ soi or $\frac{1}{\left(\frac{25}{9}\right)^{\frac{1}{2}}}$
			[3]	and M1 for at least one of 3 and 5 found

Question	n	Answer	Marks	Guida
(i)		1	2	isw conversion to decimal
		9		M1 for 9 or for $3^{-2}$ or for $\frac{1}{3}$
				Except M0 for 9 from $27/3$ or $\sqrt[3]{27}$
			[2]	
(ii)		$2a^2c^{-4}$ or $\frac{2a^2}{c^4}$ as final answer	3	B1 for each element; must be multiplied
				if B0, allow SC1 for $64a^6c^3$ obtained from numerator or for all elements correct but added
			[3]	

Question	Answer	Marks	Guidance
(i)	$-31 + 6\sqrt{5}$	3	B2 for -31 or B1 for 9 - 40 or SC1 for 49
	,		and B1 for $6\sqrt{5}$
			if 0, allow M1 for three terms correct in
		[2]	$9-6\sqrt{5}+12\sqrt{5}-40$
		[3]	
(ii)	22√2	2	M1 for $\sqrt{72} = 6\sqrt{2}$ soi or for $\frac{32}{\sqrt{2}} = 16\sqrt{2}$
			soi or for $\frac{12+32}{\sqrt{2}}$ oe
		[2]	

4x - 5 > 14x + 7	M1	for correctly multiplying by 7 to eliminate the fraction, including expanding bracket if this step done first
-12 > 10x or $-10x > 12$ or ft	M1	for correctly collecting x terms on one side and number terms on the other and simplifying
$x < -\frac{12}{10}$ or $-\frac{12}{10} > x$ oe isw or ft	M1	ft their $ax$ [inequality] $b$ , where $b \neq 0$ and $a \neq 0$ or $\pm 1$
	[3]	

(3x+1)(x+3)	M1	or $3(x+1/3)(x+3)$
		or for -1/3 and -3 found as endpoints eg by use of formula
x < -3 [or]	A1	
x > -1/3 oe	A1	mark final answers;
		allow only A1 for $-3 > x > -1/3$ oe as final answer or for $x \le -3$ and $x \ge -1/3$
		if M0, allow SC1 for sketch of parabola the right way up with their solns ft their endpoints
	[3]	•

Question	Answer	Marks	Guidance
(i)	$(3x)^2 = h^2 + (2x+1)^2$ oe	B1	for a correct Pythagoras statement for this triangle, in terms of $x$ , with correct brackets
	$9x^2 = h^2 + 4x^2 + 4x + 1$ and completion to given answer, $h^2 = 5x^2 - 4x - 1$	B1	for correct expansion, with brackets or correct signs; must complete to the given answer with no errors in any interim working may follow $3x^2 = h^2 + (2x + 1)^2$ oe for <b>B0 B1</b>
		[2]	
(ii)	$[0 = ]5x^2 - 4x - 8$	B1	for subst and correctly rearranging to zero
	$\frac{4 \pm \sqrt{(-4)^2 - 4 \times 5 \times -8}}{2 \times 5}$ or ft	M1	for use of formula in their eqn rearranged to zero, condoning one error; ft only if their rearranged eqn is a 3-term quadratic; no ft from $5x^2 - 4x - 1$ [=0]
	$\frac{4+\sqrt{176}}{10}$ or $\frac{2}{5} + \frac{\sqrt{44}}{5}$ oe	A1	isw wrong simplification;  A0 if negative root also included
		[3]	

(i)	$\left(x-\frac{5}{2}\right)^2-\frac{1}{4} \text{ oe}$	В3	B1 for $a = 5/2$ oe and M1 for $6 - their a^2$ soi;
	$\left(\frac{5}{2}, -\frac{1}{4}\right)$ oe or ft	B1 [4]	accept $x = 2.5$ , $y = -0.25$ oe

Question	Answer	Marks	Guida				
(ii)	(2, 0) and (3, 0)	B2	B1 each				
			or B1 for both correct plus an extra				
			or M1 for $(x-2)(x-3)$ or correct use of formula or for their $a \pm \sqrt{their\ b}$ ft from (i)				
	(0, 6)	B1					
	graph of quadratic the correct way up and crossing both axes	B1	ignore label of their tp; condone stopping at y-axis				

$3(x-2)^2 - 7$ isw or $a = 3$ , $b = 2$ $c = 7$ www	4	B1 each for $a = 3$ , $b = 2$ oe
		and B2 for $c = 7$ oe
		or M1 for $\left[-\right]\frac{7}{3}$ or for $5 - their\ a(their\ b)^2$
		or for $\frac{5}{3}$ – $(their b)^2$ soi B0 for $(2, -7)$
-7 or ft	B1	B0 for (2, -7)
	[5]	

n (n + 1)(n + 2) argument from general consecutive numbers leading to:	M1	condone division by $n$ and then $(n+1)(n+2)$ seen, or separate factors shown after factor theorem used;
at least one must be even	A1	or divisible by 2;
[exactly] one must be multiple of 3	A1	if M0: allow SC1 for showing given expression always even

(i)	3n isw	1
		[1]

(ii)	at least one of $(n-1)^2$ and $(n+1)^2$ correctly expanded	M1	must be seen
	$3n^2 + 2$	B1	
	comment eg $3n^2$ is always a multiple of 3 so remainder after dividing by 3 is always 2	B1	dep on previous B1  B0 for just saying that 2 is not divisible by 3  – must comment on 3n <sup>2</sup> term as well
		[3]	allow B1 for $\frac{3n^2 + 2}{3} = n^2 + \frac{2}{3}$

Question	Answer	Marks	Guida
(i)	x = 4	B1	
	(4, -3)	B1	or $x = 4$ , $y = -3$
		[2]	
(ii)	(0, 13) isw	1	or [when $x = 0$ ], $y = 13$ isw
			0 for just (13, 0) or $(k, 13)$ where $k \neq 0$
	[when $y = 0$ , ] $(x - 4)^2 = 3$	M1	or $x^2 - 8x + 13 = 0$
	$[x=]4 \pm \sqrt{3} \text{ or } \frac{8 \pm \sqrt{12}}{2} \text{ isw}$	<b>A</b> 2	need not go on to give coordinate form
	$[x-]$ 4 $\pm$ $\sqrt{3}$ or ${2}$ isw		
			A1 for one root correct
		[4]	
(iii)	replacement of $x$ in their eqn by $(x-2)$	M1	may be simplified; eg [ $y = $ ] $(x - 6)^2 - 3$
			or allow M1 for $(x - 6 - \sqrt{3})(x - 6 + \sqrt{3})$
			[=0 or y]
	completion to given answer $y = x^2 - 12x + 33$ , showing at least one correct interim step	A1	cao; condone using $f(x-2)$ in place of $y$
		[2]	

(i)	graph of cubic correct way up	B1	B0 if stops at x-axis
	crossing x-axis at $-3$ , 2 and 5	B1	on graph or nearby; may be in coordinate form
			mark intent for intersections with both axes
	crossing y-axis at 30	B1	or $x = 0$ , $y = 30$ seen if consistent with graph drawn
		[3]	
(ii)	correct expansion of two of the linear factors	M1	may be 3 or 4 terms
	correct expansion and completion to given answer, $x^3 - 4x^2 - 11x + 30$	A1	must be working for this step before given answer
		[2]	
(iii)	translation	B1	0 for shift or move etc without stating translation
	$\begin{pmatrix} 0 \\ -36 \end{pmatrix}$	B1	or 36 down, or -36 in y direction oe
		[2]	

# Statistics and probability

Question		Answer								Marks	Gu	
(i)	Upper Bound Cumulative Freq	20	30 10	40	+	60	70	_	30 19	90 120	B1	Cumulative frequencies All correct
	140 120 100						-	•			G1	For plotted points (Provided plotted at correct UCB positions)
	Cumulative Frequency  80  80  40  0  0  20		40		60		80		100		G1 G1	For joining points  (within ½ a square)  For scales
				Age							G1	For labels
										1	[5]	All marks dep on good attempt at cumulative frequency, but not cumulative fx's or other spurious values.
(ii)	Median = 45										B1	Allow answers between 44 and 46 without checking curve. Otherwise check curve.  No marks if not using diagram.
	Q1 = 37 Q3 = 53										B1	For Q3 or Q1 Allow Q1 between 37 and 38 without checking Allow Q3 between 52 and 54 without checking
	Inter-quartile range	= 53	-37	= :	16						B1	For IQR providing both Q1 and Q3 are correct
											[3]	

Question	Answer	Marks	G
(i)			Do a vertical scan and give:
	Accept	G1	First column
	0.2	G1	Second column
	0.5 Reject 0.2 Accept		Final column
	0.3 Refest 0.5 Reject		Do not award if first two
	0.4 Accept	G1	branches missing
	0.3 Patast		Branches two and three
	0.3 Retest 0.6 Reject		should come out of 'retest'
		[3]	
(ii)	$P(Accepted) = 0.2 + (0.3 \times 0.2) + (0.3 \times 0.3 \times 0.4)$	M1	For second or third product
	= 0.2 + 0.06 + 0.036 = 0.296	A1	CAO
	- 0.2 + 0.00 + 0.030 - 0.270	[2]	CAO
(iii)	P(At least one retest given accepted)	[-]	
	_ P(At least one retest and accepted)		For numerator
	P(Accepted)	M1	1 of humoruloi
	$=\frac{0.3 \times 0.2 + 0.3 \times 0.3 \times 0.4}{=0.096}$	M1	For denominator
	0.296		
	= 0.324	A1	FT their 0.296 and 0.096 Allow 0.32 with working
		[3]	

Question	Answer	Marks	Gı	
(i)	Because $P(L \mid R) \neq P(L)$	E1	If two or more methods given and only one correct, do not award the mark  Allow 0.45 ≠ 0.15	
		[1]		
(ii)	$P(L \cap R) = P(L \mid R) \times P(R) = 0.45 \times 0.22$ = 0.099	M1 A1 [2]	For product CAO	
(iii)	L R	G1	For two labelled intersecting circles, provided no incorrect labelling.	
	0.051 (0.099) 0.121	G1	For at least 2 correct probabilities. FT their $P(L \cap R)$ from part (ii) provided $\leq 0.15$	
	0.729	G1 [3]	For remaining probabilities. FT their $P(L \cap R)$ providing probabilities between 0 and 1.	

Question		Answer	Marks	
(i)	(A)	P(Watched cyc but not fb) = $\frac{15}{250} = \frac{3}{50} = 0.06$	В1	CAO (aef)
			[1]	
(i)	(B)	P(Watched one or two) = $\frac{33+12+21+14+3+65}{250}$	M1	OR: $\frac{250 - (64 + 38)}{250} =$
		$=\frac{148}{250} = \frac{74}{125} = 0.592$	A1 [2]	CAO (aef)
(ii)		P(Not watched fb watched cyc) = $\frac{15}{67}$ = 0.224 (0.223880597)	M1	
			A1 [2]	CAO (aef)

## **Kinematics**

Question	Answer	Marks	Guidance
(i)	When $t = 4$ , $s = \frac{1}{2} \times 4 \times 10$		Finding the area of the triangle or equivalent.
	s = 20	B1	
	When $t = 18$ , $s = \frac{1}{2} \times (18 + 12) \times 10$	M1	A complete method of finding the area of the trapezium or equivalent.
	s = 150	A1	CAO
		[3]	
(ii)	200 TS 150 100 100 100 100 100 100 100 100 100		
	Graph joining (0,0), (4,20) and (18, 150)	B1	Allow FT for their (4,20) and (18, 150)  Condone extension to (20, 150) with a horizontal line.
	The graph goes through (16, 140)	B1	
			Allow SC1 for the first two marks if there is a consistent displacement from a correct scale, eg plotting (18,150) at (19, 150)
	Curves at both ends	B1	The sections from $t = 0$ to $t = 4$ and from $t = 16$ to $t = 18$ are both curves
		[3]	